

# Non-linear Model Predictive Control for High-speed Autonomous Racing

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## The Project

This project aims at **developing algorithms** for **autonomous vehicles** able to **race at high speeds** and **avoid collisions** with obstacles in their environment. The high-speed environment poses a series of challenges including:

- High complexity of the dynamics that govern the car's behavior
- Increasing difficulty in achieving perfect localization

## Motivation

This study aims at making the following contributions:

- **Increasing road safety** under high-speed conditions (emergency vehicle driving)
- **Improving driver assistance technologies** (lane keeping, emergency braking, collision avoidance systems)

## Approach

The project imitates a **two-pronged approach**, with the aim of eventually merging the following directions.

- **1<sup>st</sup> Direction:** developing Non-linear Model Predictive Control algorithms that determine the behavior of the vehicle.
- **2<sup>nd</sup> Direction:** observing the limitations of hardware through the testing of fundamental perception methods on our test robot

## Methods and Results

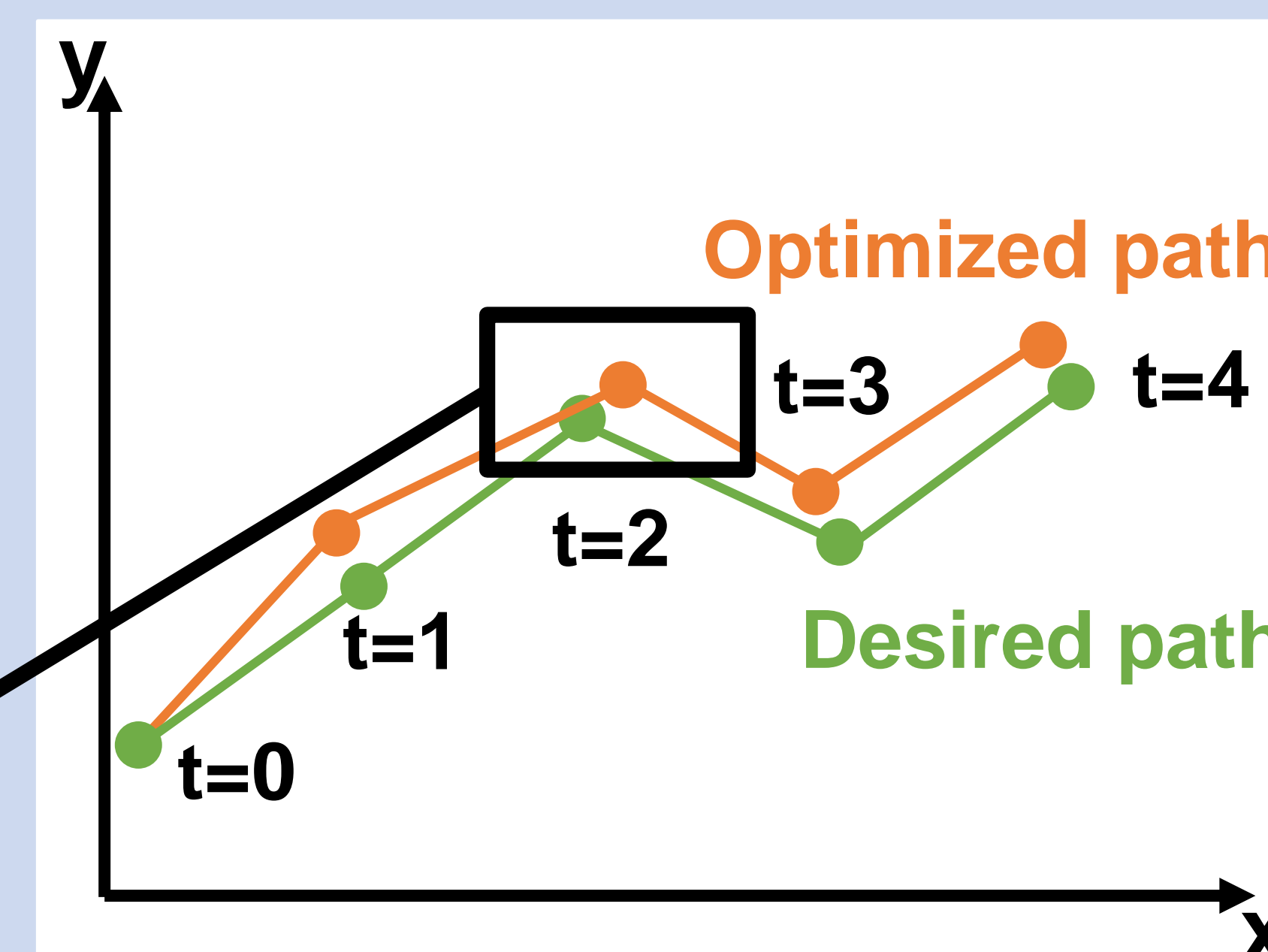
### 1<sup>st</sup> Direction - Software

Development of Non-linear Model Predictive Control algorithms (MPC), using Ipopt (optimizing software).

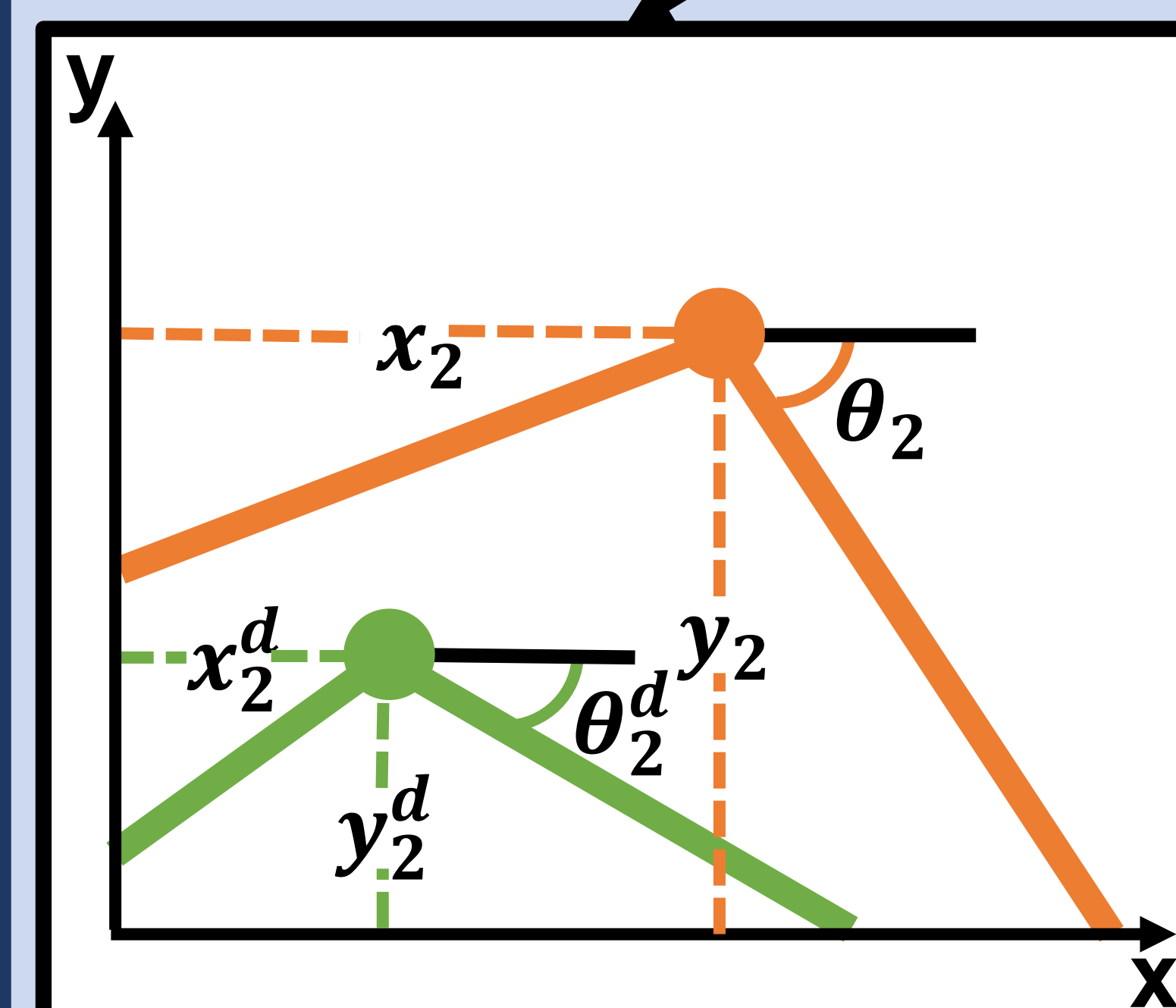
#### Characteristics and assumptions:

- Perfect localization
- Absence of other vehicles
- Small number of finite time steps
- Bicycle model
- Use of Euler's method

$$\begin{aligned}x_{t+1} &= x_t + v_t * \cos(\theta_t) & (1) \\y_{t+1} &= y_t + v_t * \sin(\theta_t) & (2) \\\theta_{t+1} &= \theta_t + \omega_t & (3)\end{aligned}$$



Figure(1): MPC finite time horizon and state (orange line: optimized path, green line: desired path)



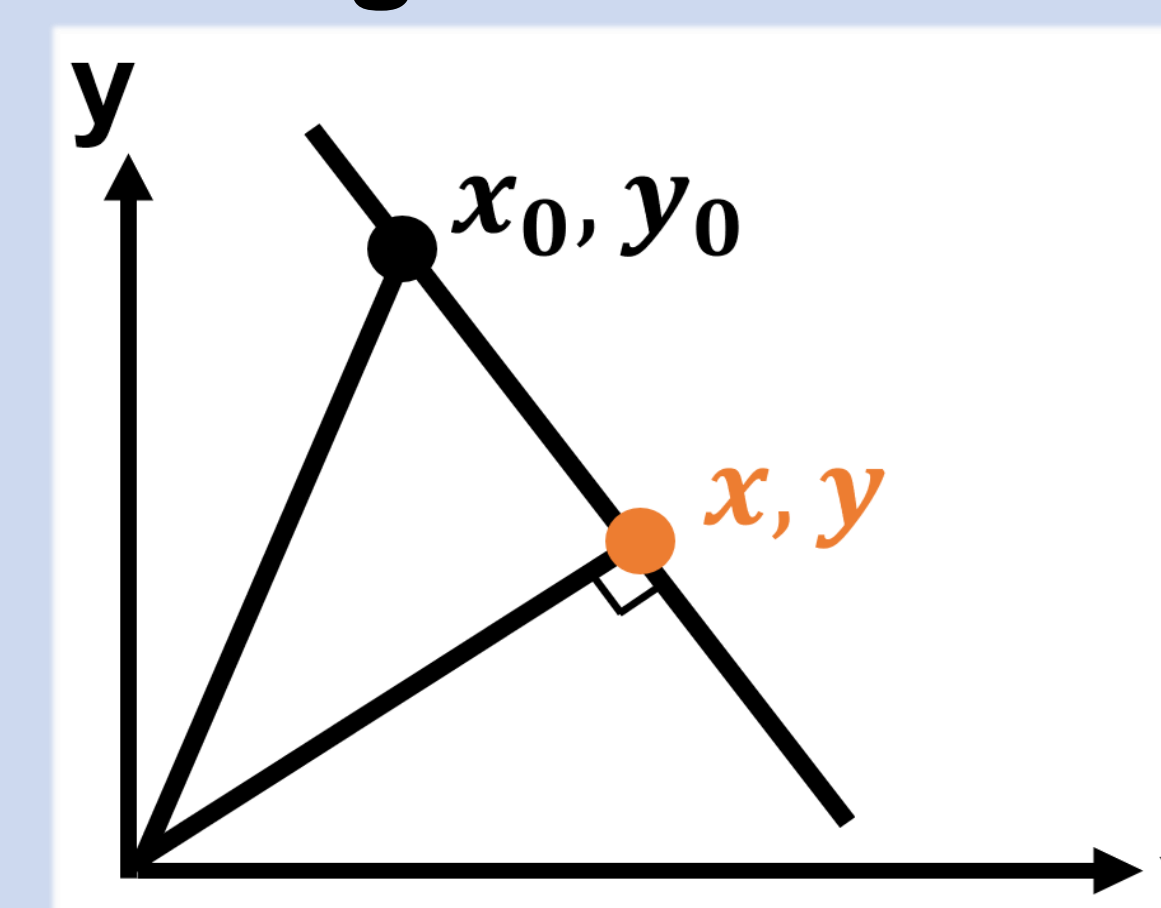
Figure(2): Magnified view of Figure(1) for t=2 focusing on the MPC optimization parameters

$$\min_{v_t, \omega_t} \sum_{t \in [0, n-1]} \left( \begin{matrix} x_t - x_t^d \\ y_t - y_t^d \\ \theta_t - \theta_t^d \end{matrix} \right)^2$$

### 2<sup>nd</sup> Direction - Hardware

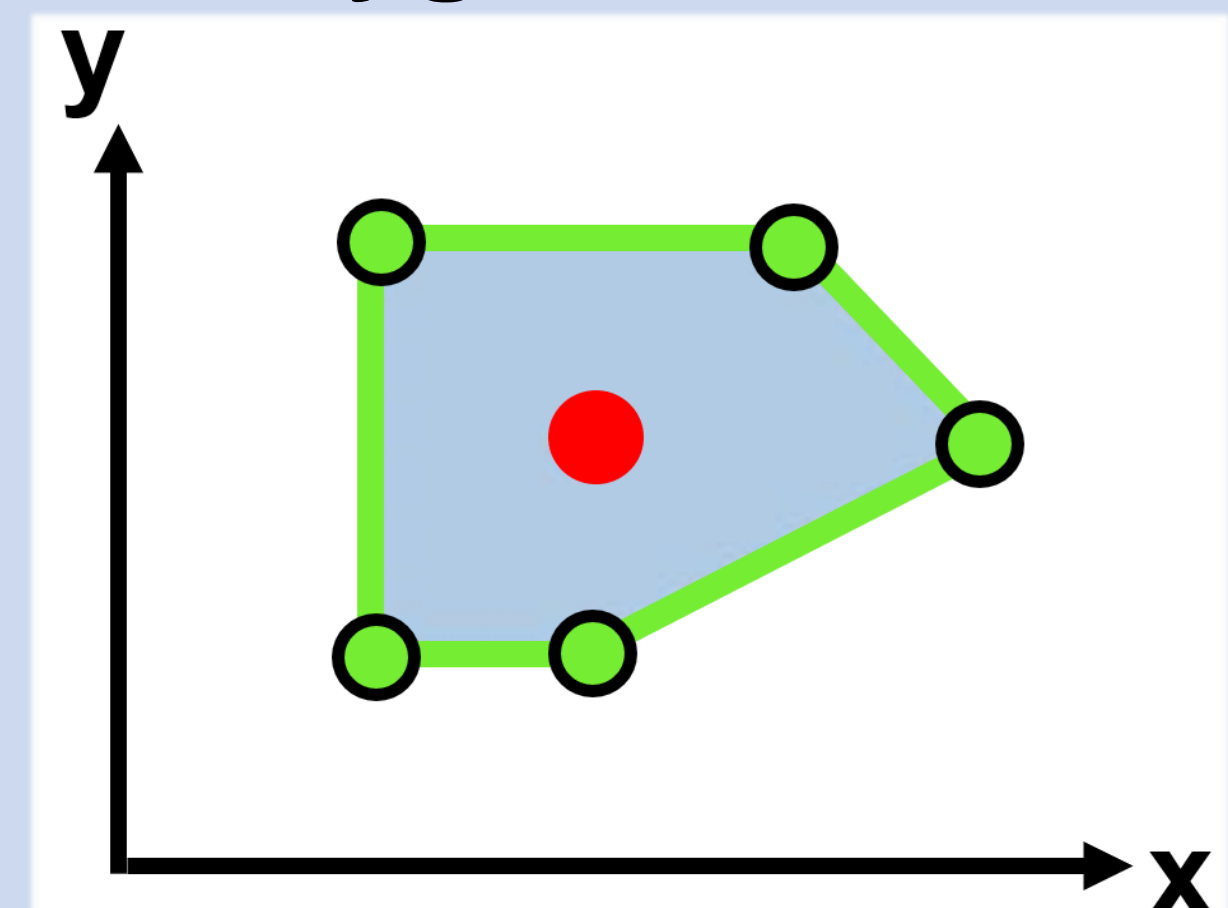
Development of a lane detection algorithm and direct implementation on our current test robot, Anki Cozmo. The following methods are used:

#### Hough Transform<sup>1</sup>



Figure(3): Line segment detection

#### Polygon Center<sup>2</sup>

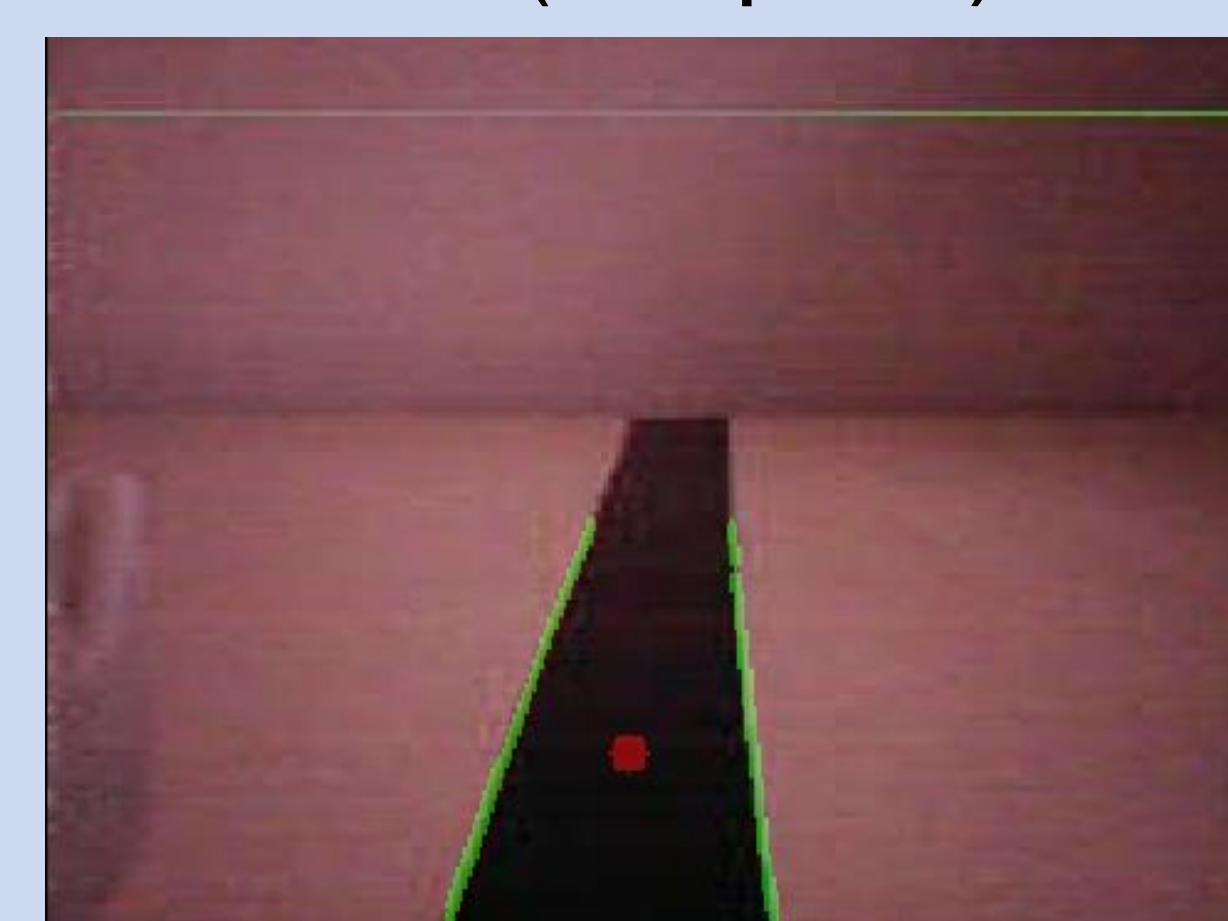


Figure(4): Center detection (red point)

#### Take-aways

- Need for high-speed calculations
- Projecting a 2D center of the lane on a 3D environment.

<sup>1</sup>Davies, Machine Vision, 2005, Chapter  
<sup>2</sup>Gillies, The Shapely User Manual, 2020



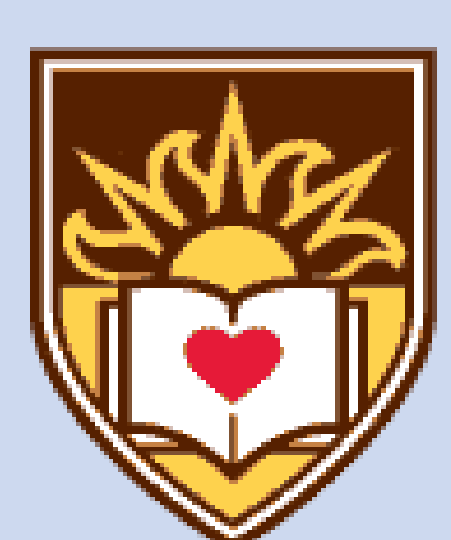
Figure(5): Image from Cozmo's view

## Next Steps / Future Work

- Integration of individual components and testing in simulation (Carla).
- Implementation of the algorithms with the aid of simulated sensors.
- Deployment of an autonomous miniature racecar based only on its onboard sensors at high speed potentially with adversarial obstacles.

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